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Mathematical modelling of hot air drying of water chestnut kernels

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Abstract

Drying characteristics of water chestnut kernels were evaluated at different air temperatures (50, 60 and 70 °C) in commercially available hot air tray dryer and sun drying. Drying rate of water chestnut kernels 1.1880, 1.6181, 2.6688 and 0.7249 g water/ g dry matter-min were found at drying temperatures of 50, 60, 70 °C and sun drying (38 ± 5 °C), respectively at 15 min time interval. The Midilli–Kucuk model fitted better on the basis of higher R² value (0.99978) and lower values of X² and RSME values as 0.0000162 and 0.004028784 at 60 °C.

Keywords: Water chestnut kernel, hot air drying, drying rate, mathematical modelling

Introduction

Water chestnut (*Trapa Natans*) belonging to the monogeneric family trapaceae. Water chestnut had been introduced as an ornamental plant by Europe. Its spreading is limited because of the large sinking nuts, but the fruit has persisted and spread northern, central and western states. It is aquatic angiospermic free floating plant which generally grown naturally in fresh water saturated land, marshes, ponds, bogs, sluggish reaches of river, swamps and brackish reaches of estuaries in both tropical and subtropical countries. It is one of the most important underutilized agricultural fruit crops. This fruit crops grow during the warmer part of the year and die out with the start of severe winter (Hummel and Kiviat, 2004) [11].

The fruit is used as a substitute for cereal in the Indian subcontinent during fasting days. In northern state of India, the harvested water chestnuts drying over mud Chulha up to 10-12 days, after that performing grinding to make flour. Rest of the place, mostly the drying of whole water chestnut is generally done by the “sun drying” method. Followed by roasting in the sand in large iron pans which account huge losses of time results less kernel recovery, low flour yield and in addition, produces the product of low quality. The dried flour is very low in fat and easily digestible and is helpful for dieting. Its flour is consumed in the form of sweet dish and for making bread, puri, halwa on several religious occasions. Besides, it has considerable importance in the manufacturing of product like biscuits; infants milk formula, starch as well as alcohol. Thus, this flour is gluten free and can be good replacement for wheat flour due to celiac disease caused by gluten intolerance. Effect of two drying temperatures 40 and 60 °C on physicochemical properties of water chestnut. The morphological characteristics of fresh starch granules were characterized by round or oval shape having diameter length ranging from 3-15 mm. After drying and rehydration at 100 °C, the granules appeared more shapeless and the surfaces were quite rough. The changes also caused more open pore volume fraction in samples dried at 60 °C, than those dried at 40 °C and many more than fresh samples. In this study, calorimetric behavior of starch and simple sugar changes after chestnut drying and rehydration were observed (Attanasio *et al.*, 2004) [2].

Drying of water chestnut slices at higher temperature and found quicker removal of water with shorter drying times. Drying rate of chestnuts was experimentally determined. The experiments were carried out in a pilot-plant scale dryer, with a closed air circuit, assisted by a heat pump. Experimental conditions were investigated; temperature (45-65 °C), relative humidity (20-40 %), and air velocity (1.8–2.7 m s⁻¹). The results show the drying rate was faster when the driving force was higher and the physical resistances were eliminated (Moreira *et al.*, 2004) [13]. Drying effect of air temperature and pretreatments on drying kinetics of other root crops like sweet potato slices and found that drying took place in the falling rate period and Page’s model was found well to describe the drying behavior (Singh *et al.*, 2006) [18].

Materials and Methods

Fully matured fresh water chestnut red variety (*Trapa natan*) was procured from local market of Dahod, Gujarat. Examined each batch of water chestnut and care was taken to have water chestnut should free from any bruised. The water chestnut corms were then washed under running portable water to remove surface dirt and then air dried.

Drying of Water Chestnut Kernels

Water chestnut kernels were dried in a tray dryer (NOVA make: Instruments Pvt. Ltd., Ahmedabad, Gujarat) at 50, 60 and 70 °C temperature at constant air velocity of 1 m/s. In each drying experiment, about 1200 g of water chestnut kernels were used. Moisture losses of samples were recorded at 15 min time intervals throughout the experiment. The experiments were repeated four times and data were recorded (Plate-1). Drying was carried out till the equilibrium moisture content achieved.

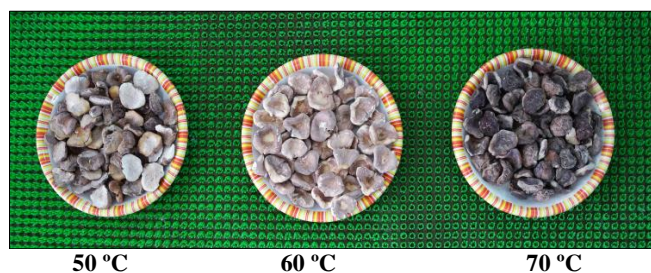


Plate 1: Dried samples of tray dryer

Open sun drying experiments were also carried out as control during month of March-April, 2020 under the clean climatic conditions at Dahod. Each experiments were started at 8.00 am and continued till 6.00 pm. To determine the moisture loss of samples during experiments, water chestnut kernels were taken out from the perforated mesh tray and weighed 20 min time interval at the beginning stage of drying to 1 h during the last stage of drying process.

Mathematical modeling of drying curves

Moisture ratio (MR) of samples was obtained using the equation as below.

$$MR = \frac{M_t - M_e}{M_0 - M_e}$$

Where M_t , M_0 and M_e are the moisture content at anytime, initial moisture content and equilibrium moisture content of samples (kg water / kg dry matter), respectively. The moisture ratio (MR) was simplified to $\frac{M}{M_0}$ instead of $\frac{M_t - M_e}{M_0 - M_e}$ by

investigator Diamante *et al.*, 1993 and Adedeji *et al.*, 2008, because fluctuation of relative humidity of the drying air. The drying rate (DR) is expressed as the amount of the evaporated moisture over time. The drying rates calculated by using the following equation.

$$DR = \frac{Mt_1 - Mt_2}{t_2 - t_1}$$

Where, t_1 and t_2 are different drying times (min) during drying; Mt_1 and Mt_2 are the moisture content of samples (kg water / kg of dry matter) at time t_1 and t_2 , respectively.

Thin layer drying models for WCK

The experimental moisture ratio data of water chestnut samples obtained were fitted to 12 most commonly used thin layer drying models. Non-linear least square regression analysis was performed using Origin pro-8 program. Three criteria of statistical analysis have been used to evaluate different models, the coefficient of determination (R^2), reduced chi-square (χ^2) and root mean square error (RMSE).

These parameters can be calculated as,

$$\chi^2 = \frac{\sum_{i=1}^N (MR_{exp,i} - MR_{pre,i})^2}{N - Z}$$

$$RMSE = \left[\frac{1}{N} \sum_{i=1}^N (MR_{pre,i} - MR_{exp,i})^2 \right]^{1/2}$$

Where, $MR_{exp,i}$ and $MR_{pre,i}$ are the experimental and predicted dimensionless moisture ratios respectively, N is number of observation and Z is number of constants in the models. For quality fit, R^2 value should be higher whereas χ^2 and RMSE should be lower.

Bulk sample of water chestnut kernels was produced using standardized pretreatment i.e 60 min in hot water treatment and 120 min residence time and optimized decorning parameter i.e. 240 rpm rotating speed of abrasive surface disk (16 no. grit size) for 14 kg feed samples and time duration 13 min. Water chestnut kernels so produced were dried under sun (as control) as well as in tray dryer at 50, 60 and 70 °C in single layer (bed thickness) in the month of March, 2020 when temperature was about 38 ± 5 °C.

Results and Discussion

The initial moisture content of water chestnut kernels was about 447.95% (db). The samples were dried to moisture content 7.71, 6.91, 5.85% and 8.62% (db) achieved at 50, 60 and 70 °C and for sun drying approx, 38 ± 5 °C, respectively. The moisture content versus drying time curves of water chestnut kernels at different temperatures are shown in Fig.1. Time required to dry the samples were 1350, 1155 and 810 min for 50, 60 and 70 °C drying temperatures respectively. While, 2640 min required to achieve EMC to sun dried sample. All the curve showed falling rate behavior and confirmed findings with Singh *et al.*, (2008) [17].

The moisture ratio progressively decreased as the drying temperature increased Fig.2. It took 310, 285, 210 and 730 min to remove the half of moisture at 50, 60, 70 °C and sun drying temperature 38 ± 5 °C, respectively which is one fourth of total drying time.

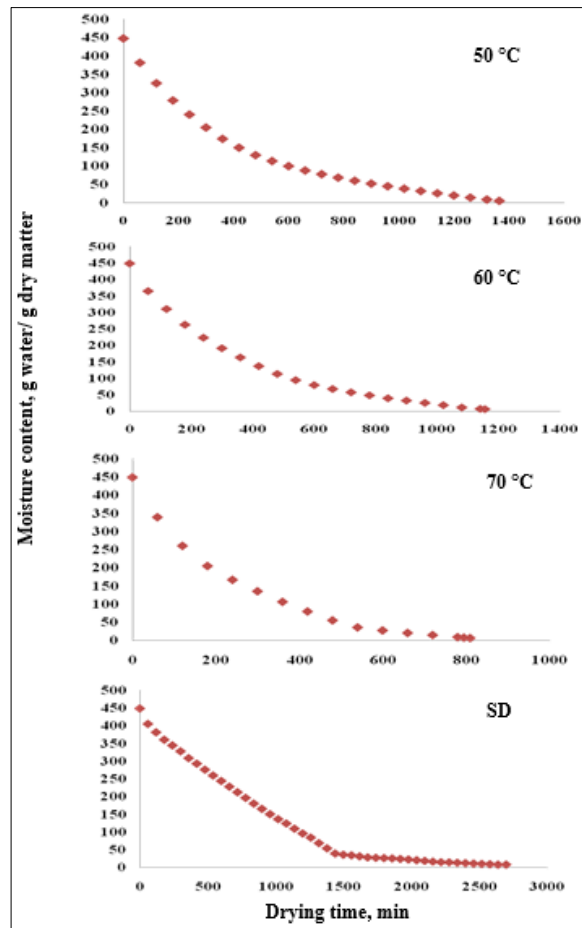


Fig 1: Moisture content versus drying time of WCK at 50, 60, 70 °C and Sun drying

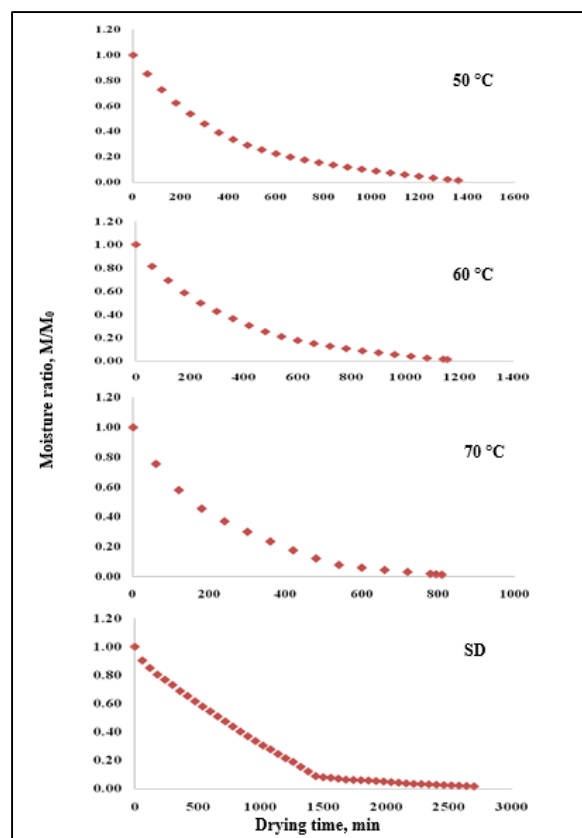


Fig 2: Moisture ratio versus drying time of WCK at 50, 60, 70 °C and Sun drying

Drying rate of water chestnut kernels 1.1880, 1.6181, 2.6688 and 0.7249 g water/ g dry matter-min were found at drying temperatures of 50, 60, 70 °C and sun drying (38 ± 5 °C),

respectively at 15 min time interval. However, the minimum drying rate was observed as low as 0.0146 g water/ g dry matter-min for sun drying condition. The average drying rate

0.3225, 0.3769, 0.5343 and 0.1517 g water/ g dry matter-min were observed at temperature 50, 60, 70 °C and sun drying conditions. The maximum drying rate was about three times more than the average drying rates. It was found that the drying rates were higher at high drying temperatures. Average drying rate increased by 16.87 %, 41.76 % and 71.60 % (Sun drying condition) for every 15 °C rise in temperature from selected temperature range 50 to 70 °C. These observations are concomitance with results reported by (Dimante and Munro, 1991) ^[5], Wang *et al.*, (2006) ^[22] and Navneet *et al.*, (2012) ^[14].

Effect of drying temperatures on drying time was found falling rate period. It can be seen that drying of water chestnut

kernels at higher temperature resulted in quicker removal of water and shorter drying times Fig.3.

It can be seen that at higher moisture content, increase in temperature has more considerable effect on the drying rates than at lower moisture content, which was negligible at the end. The reduction in drying is mainly due to reduction in moisture content as drying advances. The rate of migration of moisture from inner surface to outer surface decreases at the final stage of drying and hence, lowers drying rates. Similar results were reported by Babalis *et al.*, (2006) ^[3] for drying of figs, (Falade and Abbo, 2007) ^[7] and Rajkumar *et al.*, (2007) ^[16].

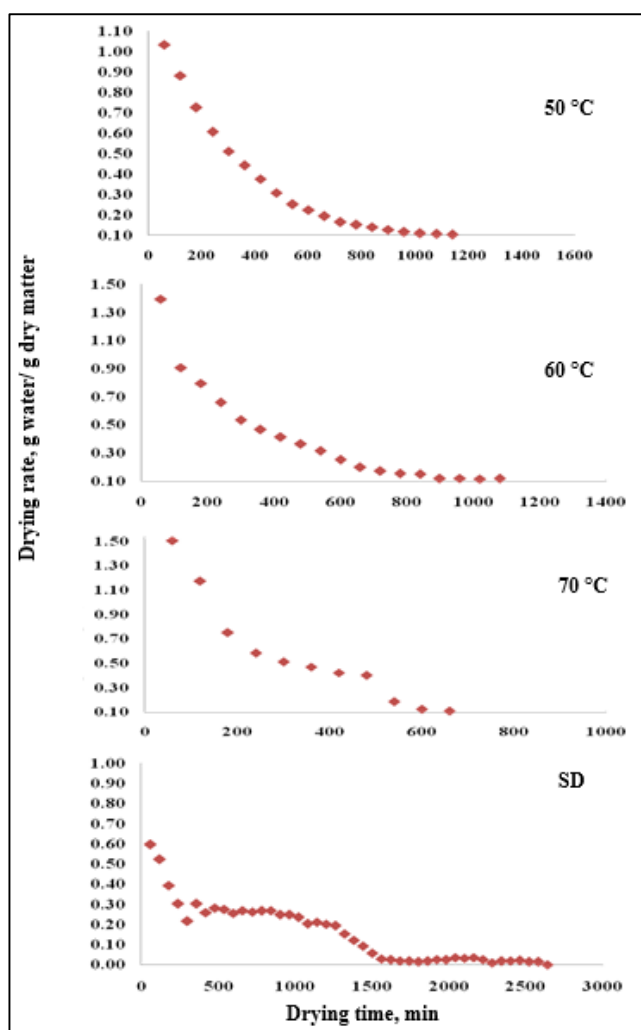


Fig 3: Drying curves of drying rate versus drying time of water chestnut kernels at 50, 60, 70 °C and Sun drying

Fitting of mathematical models to the drying curves

The moisture content data generated during drying experiments were converted into the moisture ratio (MR) and fitted to the 12 models listed in Table 1. The statistical results of the different models, including the drying model coefficients and the comparison criteria used to evaluate goodness of fit, namely R^2 , χ^2 and RSME, are listed in Table 2. Among these entire models, R^2 value was found as 0.99978 whereas χ^2 and RSME values were found lower as 0.0000565 and 0.007057, respectively.

The values of R^2 , χ^2 and RSME for all the models were ranged from 0.961 to 0.99978, 0.0000162 to 0.0027 and 0.004029 to 0.05196 with average value of 0.971257 to

0.99927, 0.0000565 to 0.00208 and 0.007057 to 0.045349, respectively (Table 5.33).

The Midilli –Kucuk model fitted better than other models on the basis of higher R^2 value (0.99978) and lower value of χ^2 and RSME as 0.0000162 and 0.004028784 at 60 °C, respectively. The residual of actual and predicted moisture ratio of Midilli –Kucuk model varied from 0.00118 to 0.00555 with an average value of 0.003587.

The selected model was established by comparing the experimental data with predicted values for each drying curve. The plotted responses (Fig.4) demonstrate the data points follow a straight line at 45 ° angle signifying the suitability of model describing the thin layer drying of water chestnut kernels. Similar approach for selecting the model for thin layer drying of fresh figs was reported by Babalis *et al.*,

(2006) [3], Singh *et al.*, (2008) [17] for water chestnut slices and Navneet *et al.*, (2012) [14] for carrot pomace.

The values of the selected model coefficients (a, k, n, c and g) for thin layer drying at 50, 60 and 70 °C were estimated. Regression analysis was performed to set up the relations between these parameters and temperatures. Thus, the second order polynomial regression equations of these constants against drying temperature T (°C) for accepted model are given below.

$$a = -160.4T^2 + 94.81T - 12.98 \quad R^2 = 1$$

$$k = 7E^{-06}T^2 - 0.000T + 0.028 \quad R^2 = 1$$

$$n = -6E^{-05}T^2 + 0.009T + 0.586 \quad R^2 = 1$$

$$b = -1E^{-08}T^2 - 9E^{-07}T + 5E^{-05} \quad R^2 = 1$$

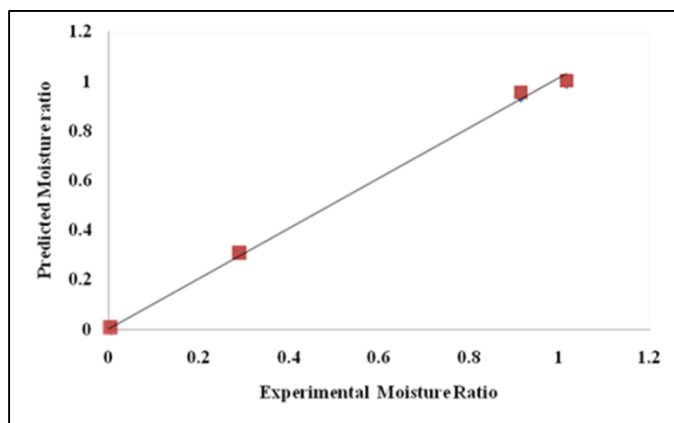


Fig 4: Predicted versus experimental moisture ratio of WCK using Midilli-Kucuk model at different drying temperatures

Table 1: Proposed thin layer drying models for water chestnut kernels (a , b , c , g , h , k , k₀ , k₁ and n : empirical constants and coefficient in drying models)

Model Name	Model Name	Model Name
Page	$MR = \exp(-kt^n)$	Page (1949) [15]
Hendersons and Pabis	$MR = a \exp(-kt)$	Hendersons and Pabis [9] (1961)
Two-Term	$MR = a \exp(k_0t) + b \exp(k_1t)$	Henderson (1974) [8]
Wang and Singh	$MR = 1 + at + bt^2$	Wang and Singh (1978) [21]
Lewis	$MR = \exp(-kt)$	Bruce (1985) [4]
Verma	$MR = a \exp(-kt) + (1-a) \exp(-gt)$	Verma <i>et al.</i> (1985) [20]
Simplified Fick's	$MR = a \exp(-c(t/L^2))$	Dimante and Munro (1991) [5]
Modified Page-II	$MR = \exp(-c(t/L^2)^n)$	Dimante and Munro (1991) [5]
Approximation of diffusion	$MR = a \exp(-kt) + (1-a) \exp(-kat)$	Yaldiz <i>et al.</i> , (2001) [23]
Logarithmic	$MR = a \exp(-kt) + c$	Togrul and Pehlivan (2002) [19]
Midilli-Kucuk	$MR = a \exp(-kt^n) + bt$	Midilli <i>et al.</i> , (2002) [12]
Hii, Law & Cloke	$MR = a \exp(-kt^n) + c \exp(-gt^n)$	Hii <i>et al.</i> , (2009) [10]

Table 2: Statistical results of the thin layer drying model coefficients at different drying temperature

Sr. No.	Model Name	Temperature °C	Constants					R ²	χ ²	RMSE
			1 st	2 nd	3 rd	4 th	5 th			
1	Lewis model	50	k=0.0261					0.9986	9.581E-05	0.009788069
2		60	k=0.00299					0.99776	1.600E-04	0.012648913
3		70	k=0.00424					0.99536	3.542E-04	0.01881991
4	Page model	50	k=0.00293	n=0.98157				0.9987	8.788E-05	0.009374359
5		60	k=0.00269	n=1.01719				0.99787	1.545E-04	0.012430326
6		70	k=0.00313	n=1.05355				0.9963	2.883E-04	0.016979812
7	Henderson Pabis	50	a=0.99118	k=0.00259				0.99869	9.094E-05	0.009536084
8		60	a=0.99502	k=0.00297				0.99779	1.601E-04	0.012653379
9		70	a=1.01228	k=0.0429				0.99553	3.482E-04	0.018661082
10	Logarithmic	50	a=0.99389	k=0.00253	c= - 0.0069			0.99876	8.667E-05	0.009309726
11		60	a=1.01274	k=0.00266	c= -0.03689			0.99951	3.620E-05	0.006016494
12		70	a=1.03582	k=0.00373	c=-0.04792			0.99854	1.159E-04	0.010766383
13	Two term	50	a=0.01032	k ₀ =484.7215	b=0.98967	k ₁ = 0.00259		0.9987	9.198E-05	0.009590766
14		60	a=0.006	k ₀ = 57.57414	b=0.994	k ₁ = 0.00297		0.99779	1.641E-04	0.012809723
15		70	a=0.03711	k ₀ = 0.00428	b=0.97515	k ₁ = 0.0429		0.99553	3.616E-04	0.019016572
16	Wang and Singh	50	a= - 0.00184	b=8.73795E-7				0.961	2.700E-03	0.051961524
17		60	a= -0.00212	b=1.15914E-6				0.97378	1.900E-03	0.043588989
18		70	a=-0.00297	b=2.24177E-6				0.97899	1.640E-03	0.040496913
19	Simple Ficks	50	a=0.99118	c=6.47461E-4				0.99869	9.094E-05	0.009536084
20		60	a=0.99498	c=7.42818E-4				0.99779	1.601E-04	0.012653379
21		70	a=1.01228	c=0.00107				0.99553	3.482E-04	0.018661082
22	Approx Diffusion	50	a=0.01053	k=0.24544				0.9987	8.987E-05	0.009479979

23		60	a=0.00596	k=0.49825				0.99779	1.597E-04	0.012637761
24		70	a=2.40203E-4	k=17.63459				0.99536	3.61E-04	0.019006394
25		50	c=7.55697E-4	n=0.9807				0.99873	8.790E-05	0.009375452
26	Modified Page II	60	c=6.81529E-4	n=1.01233				0.99786	1.55E-04	0.012454598
27		70	c=7.61407E-4	n=1.04672				0.99628	2.89E-04	0.017012966
28	Verma	50	a=-1665.3097	k=0.00261	g=0.00261			0.9986	9.798E-05	0.009898672
29		60	a=-208.63715	k=0.00369	g=0.00368			0.99814	1.37E-04	0.011696367
30		70	a=-210.50036	k=0.00568	g=0.00568			0.99675	2.58E-04	0.01606269
31	Midilli-Kucuk	50	a=1.01533	n=0.91447	b=-2.09285E-5	k=0.0043		0.99935	4.633E-05	0.006806805
32		60	a=0.99572	n=0.94204	b=-4.12398E-5	k=0.00391		0.99978	1.62E-05	0.004028784
33		70	a=1.00385	n=0.9569	b=-6.35173E-5	k=0.00501		0.99868	1.07E-04	0.01033436
34		50	a=0.71787	k=0.00293	c=0.28183	g=0.00293	n=0.98118	0.99873	9.094E-05	0.009536383
35	Hii, Law and Cloke	60	a=0.67981	k=0.002	c=0.28958	g=0.00199	n=1.06182	0.99831	1.27E-04	0.011285788
36		70	a=0.64133	k=0.00251	c=0.33569	g=0.00251	n=1.08808	0.99655	2.84E-04	0.016866446

Conclusions

Drying rates for drying of water chestnut kernels were found 1.1880, 1.6181, 2.6688 and 0.7249 g water/ g dry matter-min at temperatures of 50, 60, 70 °C and sun drying temperature (38 ± 5 °C), respectively. The average drying 0.3225, 0.3769, 0.5343 and 0.1517 g water/ g dry matter-min were observed at temperature 50, 60 & 70 °C and sun drying condition, respectively. The Midilli–Kucuk model was fitted better than other models on the basis of higher R² value (0.99978) and lower value of χ^2 and RSME value as 0.0000162 and 0.004028784 at 60 °C.

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